Programme for a rational reconstruction of ownership in PLs

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[1]: Updated from feedback, Feb. 21st.

Ownership
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Rational reconstructions
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Research questions
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Approach
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Introduction

- About resources in programming languages (an abstraction to reason about state)
- How to gain further understanding of it via models in denotational semantics
- Challenges (technical, methodological)

Introduction

Goals

- Present a set of research questions in denotational semantics motivated by language design problems
- Locate this effort within an approach to PLs that mixes data-gathering from the real world, and a critical view of the relationship between semantics and programming

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Ownership/Uniqueness

Control of aliasing

```
# let m = Array.make 4 (Array.make 4 0);;
val m : int array array =
  [|[|0; 0; 0; 0|];
    [|0; 0; 0; 0|];
    [|0; 0; 0; 0|];
    [|0; 0; 0; 0|]|]
# m.(0).(0) <- 128;;
- : unit = ()
# m;;
- : int array array =
 [|[|128; 0; 0; 0|];
   [|128; 0; 0; 0|];
   [|128; 0; 0; 0|];
   [|128; 0; 0; 0|]|]
```

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Ownership/Uniqueness

Control of aliasing

Control of aliasing

- Reasoning about state (cf. iterator invalidation)
- Concurrent programming (ownership transfer & other patterns of non-interference)
- Optimizations (C `restrict`; memory re-use)

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Ownership/Uniqueness

Resource management (bytecomp/bytelink.ml @ 8f58956 (Nov. 1996))

```
let c_file =
  Filename.chop_suffix !Clflags.object_name Config.ext_obj ^ ".c" in
if Sys.file_exists c_file then raise(Error(File_exists c_file));
try
  link_bytecode_as_c objfiles c_file;
  if Ccomp.compile_file c_file <> 0
  then raise(Error Custom_runtime);
  remove_file c_file
with x ->
  remove_file c_file;
  remove_file !Clflags.object_name;
  raise x
```

Note: example found by systematic audit of patterns of resource-management
in the OCaml compiler implementation

Ownership/Uniqueness

Resource management (bytecomp/bytelink.ml @ 40bab2d (July 2018))

```ocaml
let temps = ref [] in
Misc.try_finally
  ~always:(fun () -> List.iter remove_file !temps)
  (fun () ->
    link_bytecode_as_c tolink c_file;
    if not (Filename.check_suffix output_name ".c") then begin
      temps := c_file :: !temps;
      if Ccomp.compile_file ~output:obj_file ?stable_name c_file <> 0 then
        raise(Error Custom_runtime);
      if not (Filename.check_suffix output_name Config.ext_obj) ||
         !Clflags.output_complete_object then begin
        temps := obj_file :: !temps;
        let mode, c_libs =
          if Filename.check_suffix output_name Config.ext_obj
          then Ccomp.Partial, ""
          else Ccomp.MainDll, Config.bytecomp_c_libraries
        in
        if not (
          let runtime_lib = "-lcamlrun" ^ !Clflags.runtime_variant in
          Ccomp.call_linker mode output_name
            ([obj_file] @ List.rev !Clflags.ccobjs @ [runtime_lib])
            c_libs
        ) then raise (Error Custom_runtime);
      end
    end;
```

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Ownership/Uniqueness

Resource management

Resource management

- Memory management (malloc/free)
- Typestate/protocols
- Interoperability
- Fault tolerance (exception handling)

Ownership/Uniqueness

The Rust programming language represents a breakthrough for all these questions

- C++11 (RAII (destructors) + move semantics, among many other things): above (at an industrial scale, + structure)
- Type system for ownership & borrowing (systems programming/OOP + "linear borrows")

(Matsakis and Klock II, 2014; Anderson et al., 2016)
Like C++, it arose outside of academia

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Ownership/Uniqueness

Approaches in this area

- Linear type systems: type systems that count how many times a variable appears
  (Wadler, 1991, and others)

- Program logics, e.g. separation logic: quite successful in verifying non-toy systems including Rust
  (Reynolds, 1978; O'Hearn et al., 1999, and others)

- Ownership type systems (OOP & systems communities): greater focus on language design, more clearly a source of inspiration for Rust
  (Clarke and Wrigstad, 2003; Jim et al., 2002, and others)

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Rational reconstructions

Rational reconstructions

- Build an understanding via a refined (=épuré) model where features stand by themselves
- Connecting with existing bodies of knowledge (e.g. λ-calculus and its semantics as a bridge between intuitionistic logic and functional programming)
- Opinionated theories (not some program logics that you could apply to any programming language good or bad)

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Rational reconstructions

Example: continuations

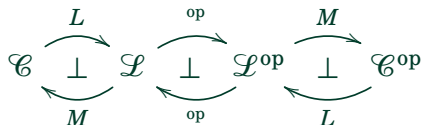*Continuations:* Historically lots of different approaches

- Semantics: categorical (monad, comonad), translations (CPS, Gödel-Gentzen, into linear logic)
- Many (!) different formalisms
- Many different questions: programming (control operators), logic (classical translations)

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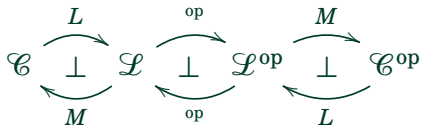# Rational reconstructions

Example: continuations

Rational reconstructions:

- Girard (1991), Danos et al. (1997): a logic that generalizes all (many) approaches
- Thielecke (1997), Levy (1999) connecting with the study of effects
- Curien and Herbelin (2000): idem for syntaxes/calculi
- Melliès: building blocks that one composes (Melliès and Tabareau, 2010)

$$\mathscr{C} \underset{M}{\overset{L}{\perp}} \mathscr{L} \underset{\mathrm{op}}{\overset{\mathrm{op}}{\perp}} \mathscr{L}^{\mathrm{op}} \underset{L}{\overset{M}{\perp}} \mathscr{C}^{\mathrm{op}}$$

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Rational reconstructions

Linear call-by-push-value

$$\mathscr{C} \underset{M}{\overset{L}{\rightleftarrows}} \bot \; \mathscr{L} \underset{\mathrm{op}}{\overset{\mathrm{op}}{\rightleftarrows}} \bot \; \mathscr{L}^{\mathrm{op}} \underset{L}{\overset{M}{\rightleftarrows}} \bot \; \mathscr{C}^{\mathrm{op}}$$
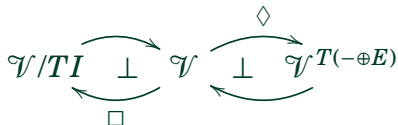
- Linear call-by-push-value (2016): how to combine *resource modalities* and *effect modalities*
- Girard: Logic of Unity (1993). Mix linear & non-linear continuations (Discussed recently: how to add duplicable continuations to OCaml?)

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Rational reconstructions

A resource modality for RAII

- Linear Call-by-push-value (2016): combination of *resource modalities* and *effect modalities*
- Combette & M. (2018). Connection between types with destructors and ordered logic.

$$\mathscr{V}/TI \quad \underset{\square}{\overset{}{\rightleftarrows}} \perp \quad \mathscr{V} \quad \underset{}{\overset{\diamond}{\rightleftarrows}} \perp \quad \mathscr{V}^{T(-\oplus E)}$$

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Rational reconstructions

A resource modality for RAII

- A type-based abstraction. Attach a destructor to a type, to create a new type.
- *Ordered* data types (rather than linear or affine)

$$A \otimes B \not\cong B \otimes A$$

- Still affine at the level of provability!

$$A \otimes B \leftrightarrow B \otimes A$$

- Solves open question of combining linearity and control effects (with lots of thanks to C++ RAII)

$$\Diamond A \rightarrow \Box(A \rightarrow \Diamond B) \rightarrow \Diamond B$$

"One needs to know how to discard a computation in order to propagate an exception"

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Rational reconstructions
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Rational reconstructions

A resource modality for RAII

"Are types in Rust linear or affine?"
Our model is clear:

- *Linear* at the level of values
- *Ordered* at the level of types
- *Affine* at the level of provability

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Rational reconstructions

A resource modality for RAII

$$\mathrm{List}(A) = \mu X.(1 \oplus (A \otimes X))$$

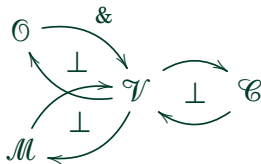$$\mathrm{Tsil}(A) = \mu X.(1 \oplus (X \otimes A))$$

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Rational reconstructions

A resource modality for RAII

$$\text{List}(A) = \mu X.(1 \oplus (A \otimes X))$$
$$\text{Tsil}(A) = \mu X.(1 \oplus (X \otimes A))$$

- The stack overflow issue
  - Open problem in C++, Rust, Swift...
  - Typed pointer reversal (solution from functional programming)

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Research questions

ML with resources?

How to add first-class resources to ML?
Mix several resources and effects in the same language


```
type t = Res u with destructor f
&t
```

e.g. Kind system inspired by polarities (Girard, 1991, 1993).

- *Qualitative* linearity (e.g. special traits in Rust), as opposed to quantitative linearity (counting how many times variables are used)
- Nevertheless expected to be compatible with lessons from affine type systems

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Research questions

Types of closures

Reconstruct what we already know
Example: types of closures

$$A \to_p B \stackrel{\text{def}}{=} \Box_p(A \to B) \qquad (p \in \{\text{M}, \text{O}\})$$

- The kind of a function does not depend on inputs and outputs
- Distinction between functions and closures
- Different kinds of closures (depending on what is in the closure)
- In Rust: Fn, FnOnce, FnMut

Research questions

Types of closures II

Making predictions

Tov and Pucella (2011): practical affine types (kind system with principal kinds)

$$t \to_{\langle \alpha \rangle} u \qquad (\langle \alpha \rangle \in \{A, U\})$$

- We do not reconstruct such a refined type system...
- ...but, they have noticed that currified functions tend to accumulate annotations in a predictable manner

$$\forall \alpha \beta (\alpha \to \beta \to_{\langle \alpha \rangle} t \to_{\langle \alpha \rangle + \langle \beta \rangle} u)$$

The model predicts a way by which by introducing explicitly a primitive ("call-by-push-value") arrow, one can remove superfluous annotations

$$\forall \alpha \beta (\alpha \rightharpoonup \beta \rightharpoonup t \rightharpoonup u)$$

(see also the treatment of currying in F#)

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Rational reconstructions
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Research questions

Rational reconstruction of ownership

Challenges to test the model
In Rust/C++, linearity and ownership are *emergent phenomena* of types with destructors (resource types/ownership types).
Other notions follow intuitively from them in Rust:

1. Region typing ("borrows"),
2. Uniqueness ("linear borrows"),
3. External uniqueness/linear abstract data types ("interior mutability").

Can this intuitive hierarchy be explained in denotational semantics?

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Rational reconstruction of ownership

Challenges to test the model

What is borrowing? How does it appear?

- Hypothesis: "&" as forgetful functor from ownership types to the base category (linear/copiable)

$$\&(A \otimes B) = \&A \otimes \&B$$

How does it prevent use-after-free if the result of a borrow is a copiable type?

- Related to a programming problem: how can I define resources starting from types all copiable?
- Hypothesis: mix of kind system + destructors + borrowing + linear abstract data types

⇒ Methodological limits to the "toy system" approach

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Rational reconstruction of ownership

Other open problems interesting to look at from this angle

- Erlang/Rust panic model
  - Ahman and Bauer (Ahman and Bauer)
- Limitations of Rust borrow checker
  - Revisit type-and-effect systems for ownership

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Challenges in language design

As you might have noticed

- Intertwined considerations from logic to computer architecture
- Requires lots of knowledge about the diverse problems faced by programmers
- Diminishing returns of the experience of writing compilers
- Limitations of the "toy language" approach
- There is more to science than making a falsifiable claim (such as type safety)
- Formal methods: how do you take into account emergent code and reasoning patterns? (cf. resource-management example at the start)

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Possible keys

This approach:

- A critical view of Curry-Howard
  (see e.g. *"the Romance of Mathematics"* about monads in Petricek, 2018)

- Allows more distance between model/toy formalism and language
  proposition, requiring a rational (not necessarily technical) discourse to
  connect to programming languages

- Responsibility for the "owners" of the means of production of knowledge
  (e.g. languages with critical mass to gather user feedback and experience)

- Go back at the roots of our belief in mathematical approaches
  (e.g. Priestley, *"The Algol Research Programme"*, 2011.)

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Possible keys
Structured programming

Structured programming (Dijkstra)

- Correctness should follow from the structure of the program
- The structures provided by the programming language should facilitate reasoning about the program

(Priestley, 2011)

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Possible keys

Structured programming

Structured programming (Dijkstra)

- Correctness should follow from the structure of the program
- The structures provided by the programming language should facilitate reasoning about the program

(Priestley, 2011)

> *"[Destructors are] a systematic approach to resource management with the important property that **correct code is shorter and less complex** than faulty and primitive approaches. [. . .]*
> *The introduction of exceptions [...] was delayed for about half a year until I found "resource acquisition is initialization" as a **systematic and less error-prone** alternative to the finally approach."*

(Stroustrup, 2007, emphasis mine)

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Possible keys

C++ as a 40-year-long experiment

"C++ is built on the idea of incremental growth and the gradual replacement of older facilities with newer ones where appropriate." (Stroustrup, 2020)
(Rust follows a similar approach.)

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Possible keys

C++ as a 40-year-long experiment

"C++ is built on the idea of incremental growth and the gradual replacement of older facilities with newer ones where appropriate." (Stroustrup, 2020)
(Rust follows a similar approach.)

A theory of programming language design and evolution

- rooted in the socio-technological context of programming languages,
- rooted both in experience *and* (to my initial surprise) the overarching research programme of our community,
- that seeks relative claims (within one language), where one cannot find evidence for absolute ones (between all languages).

Conclusion

Thank you

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